

Exercise 8.1

Q1. Given $m \overline{AC} = 1\text{cm}$, $m \overline{BC} = 2\text{cm}$, $m\angle C = 120^\circ$. Compute the length AB and the area of $\triangle ABC$.

Hint: $(\overline{AB})^2 = (\overline{AC})^2 + (\overline{BC})^2 + 2m\overline{AC} \cdot m\overline{CD}$

Where $(m\overline{CD}) = (m\overline{BC}) \cos(180^\circ - m\angle C)$ (Use theorem I)

Solution:

$$m\overline{AC} = 1\text{cm}; m\overline{BC} = 2\text{cm}; m\angle C = 120^\circ$$

Required: $m\overline{AB} = ?$

and Area of $\triangle ABC = ?$

$$\begin{aligned} m\overline{AB}^2 &= m\overline{AC}^2 + m\overline{BC}^2 + 2m\overline{AC}m\overline{CD} \\ &= (1)^2 + (2)^2 + 2(1)(\overline{CD}) \\ &= 1 + 4 + 2\overline{CD} \\ &= 1 + 4 + 2\overline{CD} \quad \text{--- (i)} \end{aligned}$$

In $\triangle BCD$,

$$m\angle BCD = 60^\circ$$

and $m\angle CBD = 30^\circ$

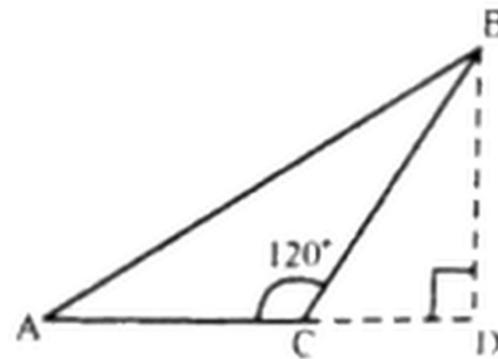
The side opposite to $\angle 30^\circ$ is \overline{CD} which is

$\frac{1}{2}\overline{CB}$, the hypotenuse of right $\triangle CDB$.

$$\overline{CD} = 1\text{cm}$$

By putting the value of \overline{CD} in eq.(1)

$$m\overline{AB}^2 = 5 + 2(1)(1) = 5 + 2 = 7$$



$$m\overline{CB}^2 = m\overline{CD}^2 + \overline{BD}^2$$

$$2^2 = 1^2 + m\overline{BD}^2$$

$$m\overline{BD}^2 = 4 - 1 = 3$$

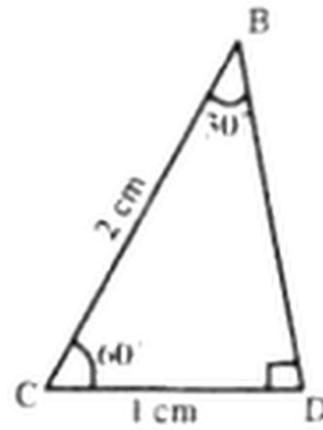
$$h = m\overline{BD} = \sqrt{3}$$

Area of ABC

$$= \frac{1}{2} \text{base} \times \text{height}$$

$$= \frac{1}{2} m\overline{AC} \times m\overline{BD}$$

$$= \frac{1}{2} \times 1 \times \sqrt{3}$$



$$\text{Area of ABC} = \frac{\sqrt{3}}{2} \text{sq cm}$$

Q2. Find $m\overline{AC}$ if in $\square ABC$ $m\overline{BC} = 6$ cm, $m\overline{AB} = 4\sqrt{2}$ cm and $m\angle ABC = 135^\circ$.

Solution:

Let $m\overline{BD} = x$

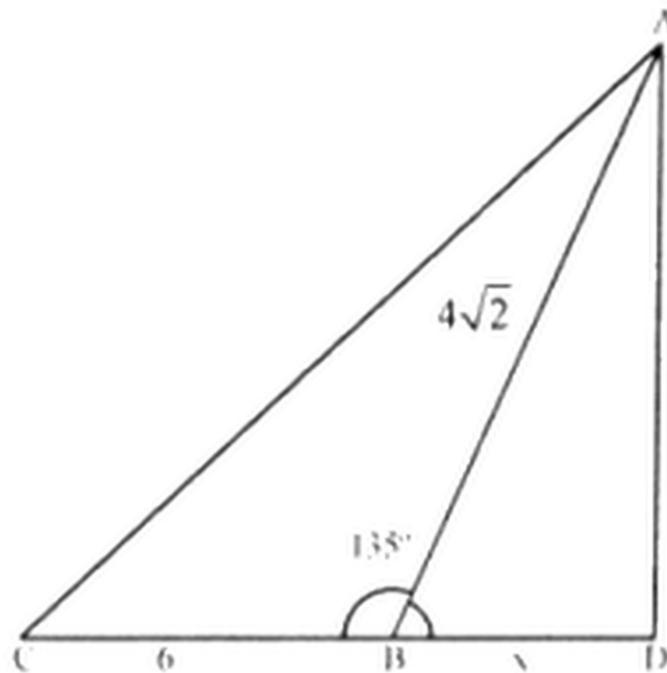
In $\square ABD$, we have

$$\cos 45^\circ = \frac{\overline{BD}}{\overline{AB}}$$

$$\frac{1}{\sqrt{2}} = \frac{x}{4\sqrt{2}}$$

$$\sqrt{2} x = 4\sqrt{2}$$

$$x = 4 \text{ cm}$$



We know that

To Prove

$$(m\overline{AC})^2 = (m\overline{CB})^2 + (m\overline{AB})^2 + 2 \times m\overline{CB} \times m\overline{BD}$$

$$\begin{aligned} &= 36 + 32 + 48 \\ &= 116 \\ \Rightarrow \overline{mAC} &= \sqrt{116} = \sqrt{4 \times 29} = 2\sqrt{29} \text{ cm} \end{aligned}$$

